# Equilibrium Price Dynamics in Perishable Goods Markets: The Case of Secondary Markets for Major League Baseball Tickets

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- aim: describe equilibrium pricing patterns and test theories of equilibrium pricing behavior in perishable goods markets
- event tickets are *perishable goods* with *fixed date consumption* 
  - worthless once the game is played
  - cannot be consumed before the game is played

## Revenue Management Models of Dynamic Pricing of Perishable Goods

- examples: McAfee and te Velde (2006), Gallego and van Ryzin (1994)
- basic theoretical structure:
  - seller starts with a given inventory and continuously varies price (no commitment)
  - · consumers arrive randomly, purchase at once or exit
  - demand parameters constant over time
  - market ends (inventory perishes) on a fixed date
- optimal price depends on probability that a current sale prevents a future one because of a stock-out
  - $\bullet~$  lower inventory  $\rightarrow~$  higher prices
  - $\bullet~$  less time remaining  $\rightarrow~$  lower prices, as future selling opportunities disappear
- a "robust prediction" (McAfee and te Velde) is that expected prices should fall over time

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# Empirical Evidence and Motivation for Looking at Secondary Ticket Markets

- little empirical work testing these models
- when declining price prediction has been tested (e.g., airlines by McAfee and te Velde), it has been rejected. Why?
  - consumer demand changes over time
  - commitment
- secondary event ticket markets have several nice features:
  - sellers are small and fairly anonymous, so commitment incentives should be small
  - most sellers offering one unit (e.g., a pair of tix), so declining price prediction emerges unambiguously

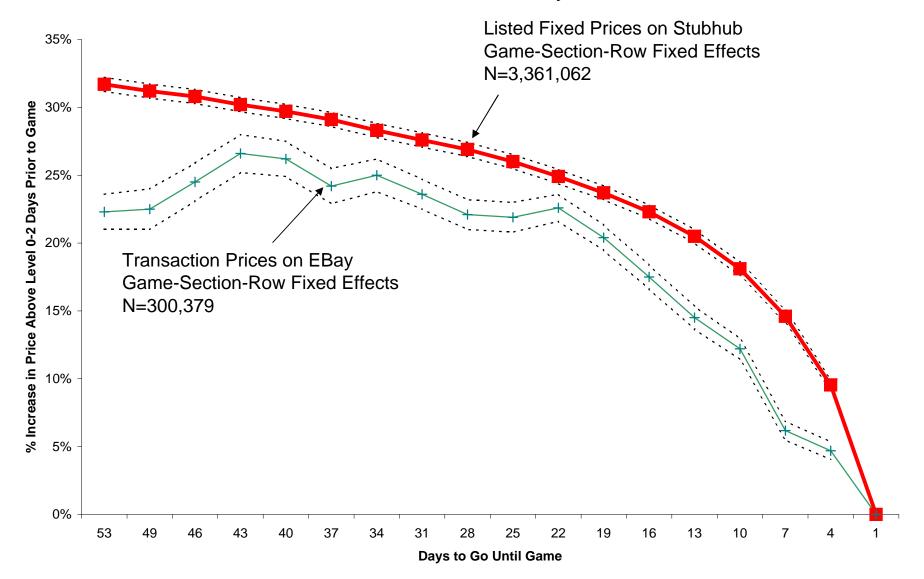
- shows, using data from two large markets, that list and transaction prices decline by significant amounts (20-50%) as the game approaches
- Ø describes three theories for why prices decline:
  - RM explanation
  - esidual demand becomes more elastic over time
  - seller learning (e.g., Lazear (1986))
- rejects 3 using reduced-form evidence; shows 1 preferred to 2 by estimating models of the seller's price-setting problem
- show most observed early purchasing rationalized by plausible 'return to market'/search costs & risk-neutrality given product differentiation and uncertainties about availability of particular types of ticket

### (Descriptive) Evidence of Price Declines

estimating equation:

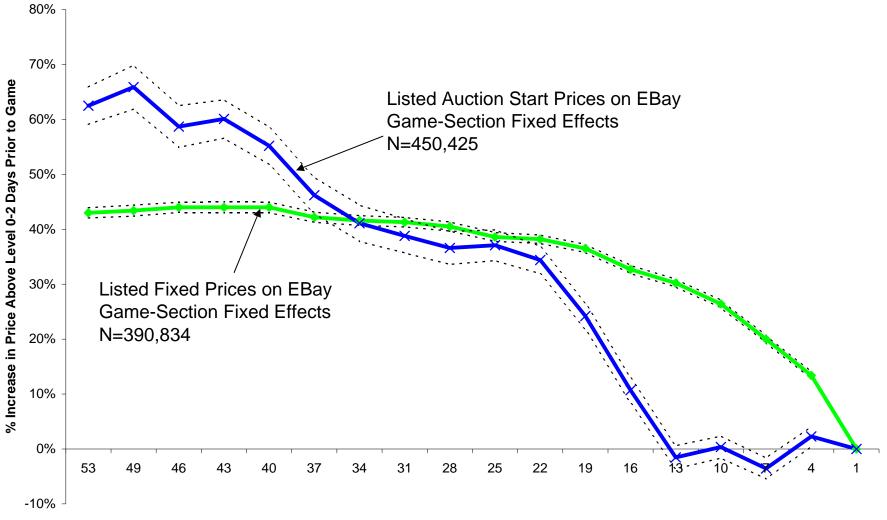
$$\begin{array}{lll} \mathsf{Price or \ Log(Price)} & = & \mathsf{DTG}\beta^{\mathsf{DTG}} + X^{\mathsf{LIST}}\beta^{\mathsf{LIST}} \\ & + X^{\mathsf{SLR}}\beta^{\mathsf{SLR}} + X^{\mathsf{FORM}}\beta^{\mathsf{FORM}} + \mathsf{FEs} + \varepsilon \end{array}$$

- measure of price:
  - buyer, seller
  - transaction, list
  - log, levels or relative to face value
- definition of fixed effects, important to control for quality:
  - game-section "Seattle Mariners at New York Yankees on May 6, Loge Box 512" and include row controls; or,
  - game-section-row; or,
  - ticket/seller-game-section



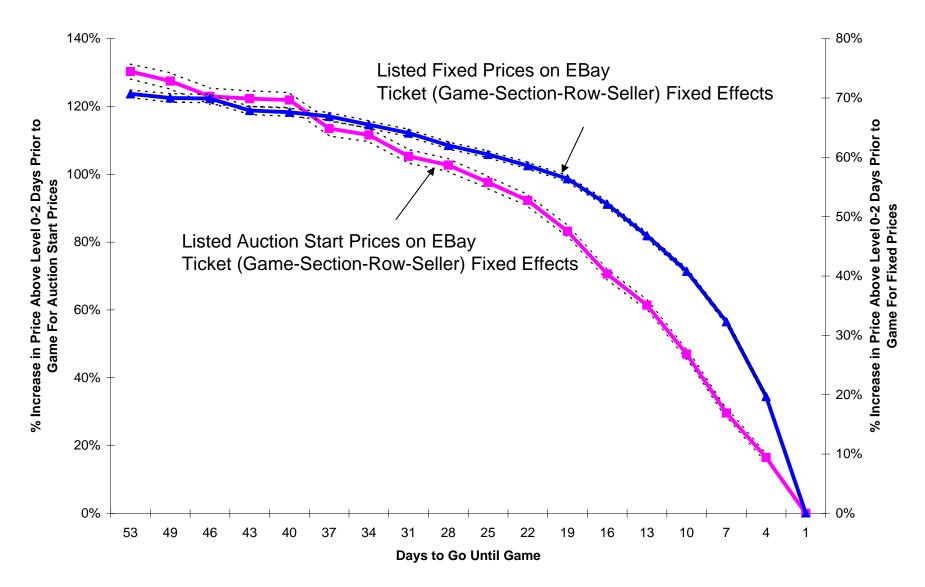
#### Price Declines in Stubhub List Prices and EBay Transaction Prices

### **EBay List Fixed Price and Auction Start Prices**



Days to Go Until Game

#### **EBay List Fixed Price and Auction Start Prices**



#### Theoretical Explanations for Why Sellers Cut Prices Explanations 1 and 2: Declining Opportunity Costs and Changing Elasticities

• fixed price listing, two periods, sets price  $p_t$ , gets v if unsold after t = 2

$$\max_{p_1,p_2} p_1 Q_1(p_1) + p_2 Q_2(p_2)(1 - Q_1(p_1)) + v(1 - Q_2(p_2))(1 - Q_1(p_1))$$

FOCs: 
$$Q_1(p_1^*) + \frac{\partial Q_1(p_1^*)}{\partial p_1} [p_1^* - (p_2^* Q_2(p_2^*) + (1 - Q_2(p_2^*))v)] = 0$$
  
 $Q_2(p_2^*) + \frac{\partial Q_2(p_2^*)}{\partial p_2} [p_2^* - v] = 0$ 

- opportunity cost of selling is v in period 2,  $p_2^*Q_2(p_2^*) + (1 - Q_2(p_2^*))v$  in period 1
- if  $Q_1(p_1) \equiv Q_2(p_2), \ p_1^* > p_2^*$
- explanation 1: prices fall because of declining opportunity costs
- explanation 2: prices fall because of changing demand elasticities

### Structural Analysis of Price Setting

Testing the Changing Demand & Declining Opportunity Cost Explanations: Example Fixed Price Listings

whenever a seller lists a ticket he is solving

$$\max_{p_{st}} p_{st} Q_{st}(p_{st}) + o_{st}(1 - Q_{st}(p_{st}))$$

where  $Q_{st}$  is the probability of sale and  $o_{st}$  is the opportunity cost of selling. If SOCs satisfied

$$p_{st}^{*} = o_{st} - \frac{Q_{st}(p_{st})}{\frac{\partial Q_{st}}{\partial p_{st}}}$$
$$\widehat{o_{st}} = p_{st} + \frac{\widehat{Q_{st}(p_{st})}}{\frac{\partial Q_{st}}{\partial p_{st}}}$$

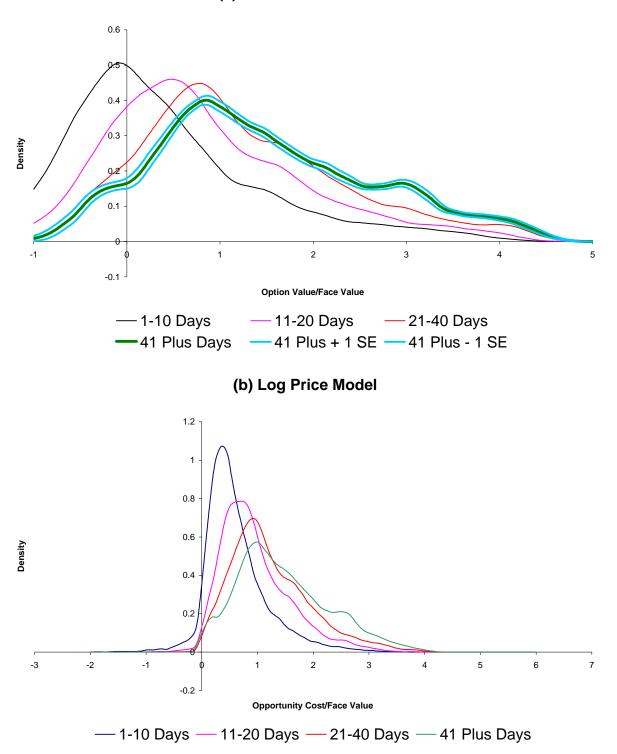
- estimate a parameterized probability of sale function (with varying elasticities)
- instrument (control function) for prices using factors affecting opportunity costs (e.g., seller distance)

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Equilibrium Price Dynamics







(a) Counterfactuals for Fixed Price Model Relative Price Model				
	Days Prior to Game			
	1-10	11-20	21-40	41 plus
<u>Actual</u>				
Mean Price	53.58	60.93	65.81	69.44
Median Price	40.63	49.50	54.20	58.50
Counterfactual: demand parameters same as 11-14 days prior to game				
competition variables same as average 11-20 days before game				
Mean Price	50.26	59.41	65.66	68.99
Median Price	39.78	49.35	55.13	59.40
(b) Counterfactuals for Fixed Price Model				
Log Price Model				
	Days Prior to Game			
	1-10	11-20	21-40	41 plus
Actual				
Mean Price	53.58	60.93	65.81	69.44
Median Price	40.63	49.50	54.20	58.50
Counterfactual: demand parameters same as 11-14 days prior to game				
competition variables same as average 11-20 days before game				
Mean Price	50.58	58.39	64.33	69.40
Median Price	40.95	49.38	54.95	59.89

- robust evidence that prices tend to decline in secondary ticket markets
- strong initial evidence that sellers cut prices because opportunity costs of selling decline as future selling opportunities disappear (because of perishability)
- early buying rational given product differentiation, plausible levels of search costs & risk aversion
- outstanding questions:
- why are price dynamics different here vs. airline/advertising markets? demand or commitment?
- What drives the choice between selling mechanisms? auctions may become more dominant because of the value of price flexibility